

Name of the Student: \_\_\_\_\_

Max. Marks : 18 Marks

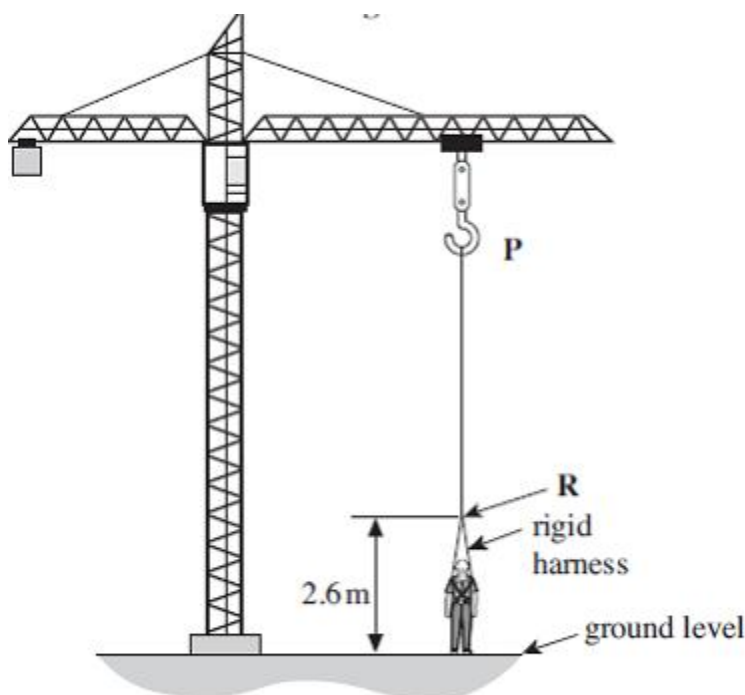
Time : 18 Minutes

**Q1.**

In a reverse bungee experience a 'rider' is catapulted high into the air. A designer creates a less extreme version for more timid participants, as shown in the figure below.

The rider is strapped into a rigid harness attached to one end of an elastic rope **PR**. The rider and the rope behave in the same way as a mass-spring system.

The rider is initially held at rest at ground level. The top end of the rope, **P**, is raised to stretch the rope. The rider is then released and moves upwards, reaching a maximum height when the rope is at its unstretched (natural) length. The rider then oscillates vertically until eventually coming to rest, suspended above the ground.



The rope has an unstretched length of 20 m. When stretched, the rope obeys Hooke's law and has a stiffness of  $92 \text{ Nm}^{-1}$ . In the following questions ignore the mass of the rope.

- (a) (i) The rider and harness have a total mass of 55 kg.  
Calculate the overall length of the rope when the rider comes to rest, suspended above the ground, at the end of the ride.

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overall length \_\_\_\_\_ m

(3)

- (ii) At the start of the ride, the lower end of the rope **R** is attached to the rigid harness at a point which is 2.6 m above the ground.

The top end of the rope, **P**, has to be adjusted so that the rope just becomes unstretched when the rider is at the highest point of the ride.  
Determine the height of **P** above the ground.  
Neglect air resistance in this part of the question.

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height of point **P** \_\_\_\_\_ m

(1)

- (b) (i) Show that the frequency of oscillation of the rider on the end of the rope is about 0.2 Hz.

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(3)

- (ii) Calculate the maximum speed reached by the rider when the amplitude of the oscillation is 4.2 m.

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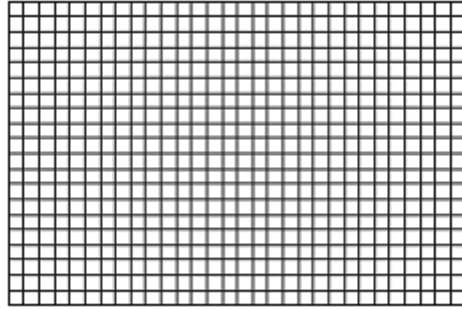
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maximum speed \_\_\_\_\_  $\text{ms}^{-1}$

(2)

- (iii) In practice, air resistance has an effect. Sketch below, a graph showing how you would expect the velocity to vary with time over the first two complete oscillations, from the instant the rider was released from ground level. Take an upward velocity as being positive.

Label the time axis with a suitable scale. No scale is required on the velocity axis.



(3)

- (c) (i) A rider of greater mass now uses the ride. Explain how the height of **P** has to be changed to produce the same initial amplitude of oscillations as that for the previous rider.

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(3)

- (ii) A safety officer examines the design of the ride and thinks that, if the end **P** of the rope is raised too high so that the rope is stretched too much at the start, there is a risk that the rider could hit the ground after the first oscillation and suffer an injury. Describe what would happen to the rider during the ride in this case and explain why, even if air resistance is negligible, the safety officer's concerns are unfounded.

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(3)

(Total 18 marks)