

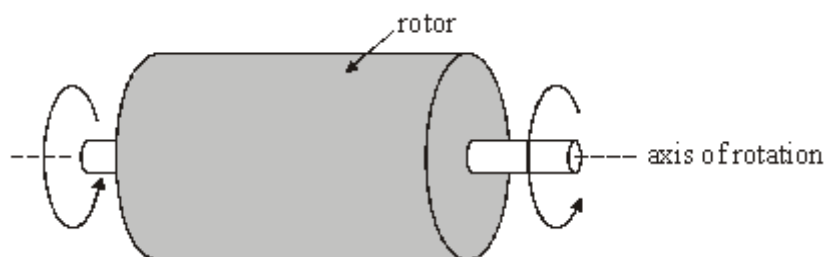
Name of the Student: \_\_\_\_\_

Max. Marks : 23 Marks

Time : 23 Minutes

**Q1.**

'Low inertia' motors are used in applications requiring rapid changes of speed and direction of rotation. These motors are designed so that the rotor has a very low moment of inertia about its axis of rotation.



- (a) (i) Explain why a low moment of inertia is desirable when the speed and direction of rotation must be changed quickly.

---

---

---

---

- (ii) State, giving a reason in each case, **two** features of rotor design which would lead to a low moment of inertia about the axis of rotation.

---

---

---

---

(4)

- (b) In one application, a rotor of moment of inertia  $4.4 \times 10^{-5} \text{ kg m}^2$  about its axis of rotation is required to reverse direction from an angular speed of  $120 \text{ rad s}^{-1}$  to the same speed in the opposite direction in a time of 50 ms. Assuming that the torque acting is constant throughout the change, calculate

- (i) the angular acceleration of the rotor,

---

---

(ii) the torque needed to achieve this acceleration,

---

---

(iii) the angular impulse given to the rotor during the time the torque is acting,

---

---

(iv) the angle turned through by the rotor in coming to rest momentarily before reversing direction.

---

---

(4)

(Total 8 marks)

**Q2.**

An early form of four-stroke gas engine stores kinetic energy in a large flywheel driven by the crankshaft. The engine is started from rest with its load disconnected and produces a torque which accelerates the flywheel to its off-load running speed of  $110 \text{ rev min}^{-1}$ .

(a) The flywheel has a moment of inertia of  $150 \text{ kg m}^2$  and takes 15 s to accelerate from rest to an angular speed of  $110 \text{ rev min}^{-1}$ .

(i) Show that the rotational kinetic energy stored in the flywheel at this speed is approximately 10 kJ.

---

---

---

(ii) Calculate the average useful power output of the engine during the acceleration.

---

---

(iii) Use your answer to part (ii) to calculate the average net torque acting on the flywheel during the acceleration.

---

---

(5)

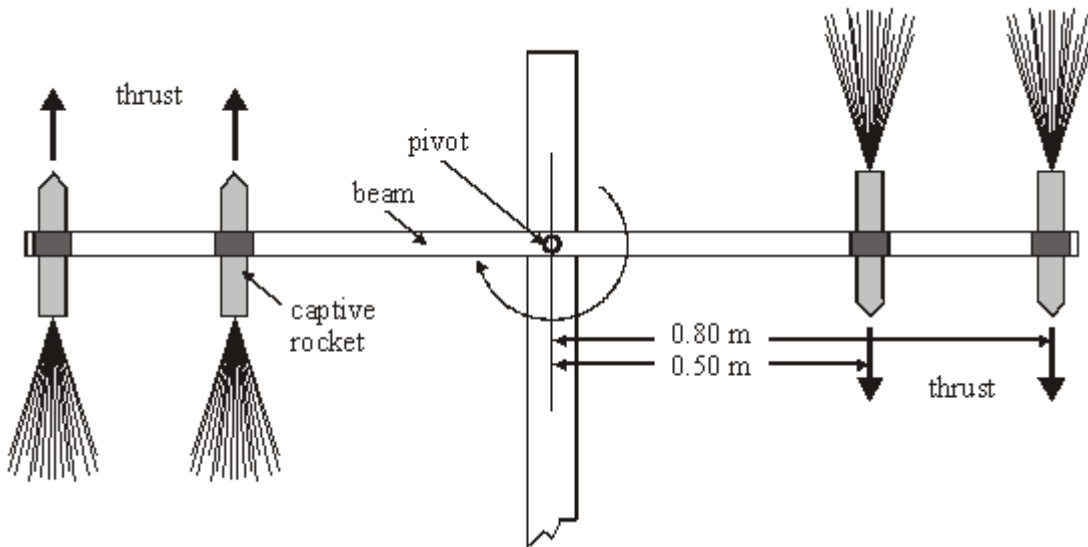
(b) When the engine is running at  $110 \text{ rev min}^{-1}$  off-load, the gas supply to the engine is suddenly cut off and the flywheel continues to rotate for a further 35 complete turns before coming to rest. Calculate the average retarding torque acting on the flywheel.

---

---

**Q3.**

**Figure 1** shows a 'firewheel' used at a firework display. Thrust produced by the captive rockets creates a torque which rotates the beam about a horizontal pivot at its centre. The shower of brilliant sparks in the exhaust gases of the rapidly orbiting rockets creates the illusion of a solid wheel.



**Figure 1**

- (a) The rockets are fixed symmetrically about the pivot at distances of 0.50 m and 0.80 m from the pivot. The initial mass of each rocket is 0.54 kg and the moment of inertia of the beam about the pivot is 0.14 kg m<sup>2</sup>.

Show that the initial moment of inertia of the firewheel about the pivot is 1.10 kg m<sup>2</sup>.

---

---

---

(2)

- (b) The rockets are ignited simultaneously and each produces a constant thrust of 3.5 N. The frictional torque at the pivot is negligible. Calculate

- (i) the total torque about the pivot when all the rockets are producing thrust,

---

---

- (ii) the initial angular acceleration of the firewheel,

---

---

- (iii) the time taken for the firewheel to make its first complete turn, starting from rest.

---

---

---

(4)

- (c) The total thrust exerted by the rockets remains constant as the firewheel accelerates. Explain why, after a short time, the firewheel is rotating at a constant angular speed which is maintained until the rocket fuel is exhausted.

---

---

---

---

---

(2)

(Total 8 marks)