

Name of the Student: \_\_\_\_\_

Max. Marks : 25 Marks

Time : 25 Minutes

Mark Schemes

Q1.

Question Number	Answer	Mark
(a)(i)	Use of $\omega = \frac{2\pi}{T}$ (1) See $F = \frac{GMm}{r^2}$ and $F = m\omega^2 r$ (1) $GM = 4.07 \times 10^{14} \text{ (m}^3 \text{ s}^{-2}\text{)}$ (1)  Or Use of $v = \frac{2\pi r}{T}$ (1) See $F = \frac{GMm}{r^2}$ and $F = \frac{mv^2}{r}$ (1) $GM = 4.07 \times 10^{14} \text{ (m}^3 \text{ s}^{-2}\text{)}$ (1) [If reverse "show that" attempted, max 2]  <u>Example of calculation:</u> $\omega = \frac{2\pi}{T} = \frac{2\pi \text{ rad}}{2.36 \times 10^6 \text{ s}} = 2.66 \times 10^{-6} \text{ rad s}^{-1}$ $\frac{GMm}{r^2} = m\omega^2 r$ $GM = \omega^2 r^3 = (2.66 \times 10^{-6} \text{ s}^{-1})^2 \times (3.86 \times 10^8 \text{ m})^3 = 4.07 \times 10^{14} \text{ m}^3 \text{ s}^{-2}$	3
(a)(ii)	Use of $g = \frac{GM}{R^2}$ with $g = 9.81 \text{ N kg}^{-1}$ (1)  $R = 6.4 \times 10^6 \text{ m}$ [ $6.5 \times 10^6 \text{ m}$ if show that value used] (1)  <u>Example of calculation:</u> $R = \sqrt{\frac{GM}{g}} = \sqrt{\frac{4.07 \times 10^{14} \text{ m}^3 \text{ s}^{-2}}{9.81 \text{ N kg}^{-1}}} = 6.44 \times 10^6 \text{ m}$	2

(b)	Force varies with distance (from the Earth) according to inverse square law $F \propto \frac{1}{r^2}$	(1)	
	so force (on these asteroids) is (very) small	(1)	
	<b>Or</b> Gravitational field strength varies with distance (from the Earth) according to inverse square law $g \propto \frac{1}{r^2}$	(1)	
	so gravitational field strength is (very) weak at this distance	(1)	2
	[Accept idea that since the asteroids are much further from the Earth (than the moon) they are only weakly bound (to the Earth) for max 1 mark]		
	<b>Total for Question</b>		7

Q2.

Question Number	Answer	Mark
	Use of $F = \frac{Gm_1m_2}{r^2}$	(1)
	$F = 8.2 \times 10^{16} \text{ N}$	(1)
	<u>Example of calculation:</u> $F = \frac{Gm_1m_2}{r^2} = \frac{6.67 \times 10^{-11} \text{ Nm}^2 \text{ kg}^{-2} \times 6.4 \times 10^{23} \text{ kg} \times 6.0 \times 10^{24} \text{ kg}}{(5.6 \times 10^{10} \text{ m})^2}$ $F = 8.17 \times 10^{16} \text{ N}$	
		2

Q3.

Question Number	Answer	Mark
	B	1

Q4.

Question Number	Acceptable answers	Additional guidance	Mark
i	<ul style="list-style-type: none"> <li>Use of <math>\omega = 2\pi/T</math> (1)</li> <li>For at least 2 full cycles (1)</li> <li><math>\omega = 6.5 \times 10^{-6}</math> (radian <math>s^{-1}</math>) (1)</li> </ul>	For MP3, accept correctly rounded answers in range $6.5 \times 10^{-6}$ radian $s^{-1}$ to $6.6 \times 10^{-6}$ radian $s^{-1}$ <u>Example of calculation</u> $\omega = 5 \times 2\pi / (56 \times 24 \times 60 \times 60) \text{ s}$ $= 6.49 \times 10^{-6} \text{ radian } s^{-1}$	3
ii	<ul style="list-style-type: none"> <li>Equates <math>F = Gm_1m_2/r^2</math> and <math>F = m\omega^2r</math> (1)                Or <math>F = Gm_1m_2/r^2</math> and <math>F = mv^2/r</math> with <math>v = 2\pi r/T</math> (1)</li> <li>Correct rearrangement and substitution (e.g. in <math>r^3 = Gm_1/\omega^2</math>) (1)</li> <li><math>r = 7.2 \times 10^9 \text{ m}</math> (ecf from (b)(i))</li> </ul>	<u>Example of calculation</u> $r^3 = 6.67 \times 10^{-11} \text{ N m}^2 \text{ kg}^{-2} \times 0.12 \times 1.99 \times 10^{30} \text{ kg} / (6.5 \times 10^{-6} \text{ radian } s^{-1})^2$ $r = 7.2 \times 10^9 \text{ m}$ ( $r = 7.6 \times 10^9 \text{ m}$ for 'show that' value)	3

Q5.

Question Number	Answer	Mark
(a)	Use of $F = \frac{Gm_1m_2}{r^2}$ (1) $G = 6.6 \times 10^{-11} \text{ (N m}^2 \text{ kg}^{-2})$ [must see $6.6 \times 10^{-11}$ when rounded to 2 sf] (1) <u>Example of calculation</u> $G = \frac{1.5 \times 10^{-7} \text{ N} \times (0.23 \text{ m})^2}{160 \text{ kg} \times 0.75 \text{ kg}} = 6.61 \times 10^{-11} \text{ N m}^2 \text{ kg}^{-2}$	2
(b)(i)	Read (peak) times from graph for at least 3 cycles (1) $T = 6.4 \text{ min } (\pm 0.2 \text{ min})$ [T = (380 $\pm$ 12) s] (1) [max 1 mark if correct answer shown without working] <u>Example of calculation</u> $T = \frac{(28.0 - 2.5) \text{ min}}{4} = 6.38 \text{ min}$	2
(b)(ii)	Air resistance acts on the sphere [accept frictional forces Or (viscous) drag for air resistance] (1) Energy is removed from the oscillation/system Or the oscillation/system is damped (1) [For mp 2 do not credit 'energy is lost' but accept 'energy is dissipated'; answer must indicate idea of transfer of energy]	2

<b>(b)(iii)</b>	<p>Evidence of values of at least 3 consecutive peaks read from graph [accept values of 3 points separated by equal time intervals] (1)</p> <p>Attempt to obtain amplitudes, by subtracting 0.75 (1)</p> <p>Calculation of two values of <math>A_{n+1}/A_n</math> with corresponding conclusion  <b>Or</b> Calculation of two values of difference of <math>\ln A_{n+1}</math> and <math>\ln A_n</math> with corresponding conclusion (1)</p> <p><b>Or</b>  Use peaks of graph to sketch curve (1)  Use curve to determine "half-life" [accept other ratio] (1)  Calculation of two values of "half-life" with corresponding conclusion (1)</p> <p><u>Example of calculation</u>  <math>A_0 = 1.45 - 0.75 = 0.7</math>, <math>A_1 = 0.75 - 0.25 = 0.5</math>, <math>A_2 = 1.1 - 0.75 = 0.35</math>, <math>A_4 = 0.75 - 0.5 = 0.25</math></p>		<b>3</b>
	$\frac{A_1}{A_0} = \frac{0.50}{0.70} = 0.71$ $\frac{A_2}{A_1} = \frac{0.35}{0.50} = 0.70$ $\frac{A_3}{A_2} = \frac{0.25}{0.35} = 0.71$		
<b>Total for question</b>			<b>9</b>