

Name of the Student: _____

Max. Marks : 26 Marks

Time : 26 Minutes

Mark Schemes

Q1.

- (a) energy supplied/transferred/input to system/gas (by heating/heat transfer) ✓

OR

energy transferred/lost/output from system/gas (by cooling heat transfer) if Q negative

*Do not allow 'heat' in place of 'energy'**Do not accept 'heat transferred' on its own**Accept 'heat energy supplied' but not 'heat supplied'.*

1

- (b) Tick against top line only

-10.8 0 10.8

1

- (c) Use of
- $p_1 V_1^{1.4} = p_2 V_2^{1.4}$
- ✓

'use of' means by substitution or manipulation to make p_2 the subject of

$$p_1 \left(\frac{V_1}{V_2} \right)^{1.4}$$
the equation eg $p_2 =$ seen
Accept γ for 1.4.
Giving $p_2 = 2.32 \times 10^6$ (Pa) ✓

$$T_2 \left(= \frac{p_2 V_2 T_1}{p_1 V_1} \right) = 710(\text{K}) \quad \checkmark$$

$$T_2 = \frac{2.32 \times 10^6 \times (3.19 \times 10^{-9}) \times 293}{1.05 \times 10^5 \times 2.91 \times 10^{-8}}$$

$$T_2 = \frac{2.32 \times 10^6 \times (3.19 \times 10^{-9}) \times 293}{1.05 \times 10^5 \times 2.91 \times 10^{-8}}$$

ECF for T_2 using their p_2

3

- (d) Slow change means internal energy remains (nearly) constant due to energy loss by heat transfer

OR

Slow change means (nearer to) isothermal change ✓

(Therefore)

the work done would be lower because the area under the graph would be lower

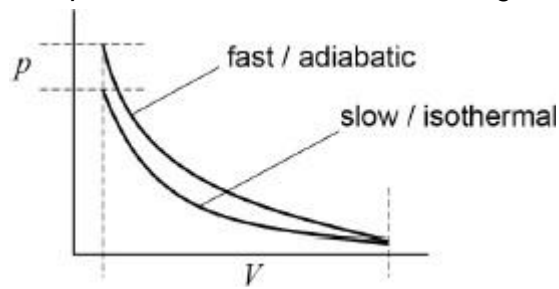
OR

the work done would be lower because the pressures are lower ✓

(Therefore, cyclist is not correct)

Allow reverse argument from fast change perspective.

Accept answers where shown in a diagram:



Alternative MP2: smaller (average) p for same ΔV will give less W

Max 2

[7]

Q2.

- (a) Attempt at calculating area above or below t axis or both ✓

(Ang displacement =) $2.80 + 2.10 - 3.15 = 1.75$ rad

$(\frac{1.75}{12.0}) = 0.15$ (rad s⁻¹) ✓

Method must be valid

MP2: correct answer only

(calculator value = 0.145833)

MAX1 if counting square method used and answer rounds to 0.15 (rad s⁻¹)

2

- (b) $P = T\omega$ giving 546 (W) ✓

Allow ecf for 590 (W) from

using $\omega_1 = 1.5$ rad s⁻¹

1

- (c) Selects steepest part of graph and

determines gradient $\alpha = \frac{1.40 - -0.90}{5.0} = 0.46$ (rad s⁻²) ✓₁

$T = I\alpha = 9660$ N m ✓₂

Adds friction torque to give 10 100 (N m) ✓₃

Accept any correct calculation of steepest graph slope: eg from 2 s to 5 s

$$\alpha = \frac{1.4}{3.0} = 0.467 \text{ giving } T = 9800 \text{ N m}$$

or 5 s to 7 s

$$\alpha = \frac{0.9}{2.0} = 0.45 \text{ giving } T = 9450 \text{ N m}$$

Allow ECF from MP2 to MP3

(d) (net) $T \times t = 9660 \times 5.0 = 4.8 \times 10^4$ (N m s) ✓

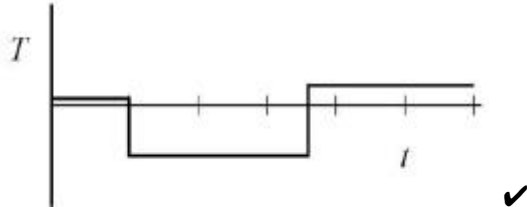
OR

$$\Delta(I\omega) = 2.1 \times 10^4 (1.40 - (-0.90)) = 4.8 \times 10^4 \text{ (N m s)} \quad \checkmark$$

For first method allow ECF for torque ✓₂ from (c), but not for ✓₃ value
(calculator value = 48300)

1

(e)



Tick (✓) against 3rd box

1

[8]

Q3.

- (a) Attempt to use work done = force × distance with either incline work or resistance work or both ✓₁

Work done by flywheel

$$= [(1.46 \times 10^4 \times 9.81 \times \sin 5^\circ) + 1.18 \times 10^3] \times 500 \quad \checkmark_2$$

$$(\text{= } 6.83 \times 10^6 \text{ J})$$

$$\frac{1}{2} I\omega^2 = 6.83 \times 10^6 \text{ giving } \omega = 468 \text{ (rad s}^{-1}\text{)} \quad \checkmark_3$$

MP1: award mark for valid attempt to calculate

mgh or $F \times s$ or both

$$mgh = 6.24 \times 10^6 \text{ J}$$

$$F \times s = 5.9 \times 10^5 \text{ J}$$

MP2 for correct calculation of work done

MP3 for using their work done and $\frac{1}{2} I\omega^2$ to calculate ω

ECF for ✓₃

3

- (b) ✓₁ for idea of use of flywheel as brake

✓₂ for idea of storing and reusing this energy

E_p change of tram can be converted to E_k of flywheel so less energy transferred to brakes/brakes last longer/tram will not reach a high speed ✓₁

OR

Energy otherwise dissipated/lost in brakes can be fed back to flywheel

✓₁

Fly wheel is charged/stores energy and energy can be used for later acceleration/driving ✓₂

OR

Fly wheel is charged/stores energy and at next stop less recharging energy will be needed. ✓₂

Give two marks if both points covered in their answer to part 1

Treat as neutral answers in terms of providing a smoother ride or less wear on parts due to connecting and reconnecting flywheel.

If no other marks are given, allow 1 MAX for a correct reference to regenerative braking.

2

- (c) **The mark scheme gives some guidance as to what statements are expected to be seen in a 1 or 2 mark (L1), 3 or 4 mark (L2) and 5 or 6 mark (L3) answer. Guidance provided in section 3.10 of the 'Mark Scheme Instructions' document should be used to assist in marking this question.**

Mark	Criteria
6	The factors which affect E_k and all three areas of shape, material and design for high ω will be covered in some detail. 6 marks can be awarded even if there is an error and/or if parts of one aspect are missing.
5	The factors which affect E_k and all three areas will be covered, at least two in detail.
4	Two areas successfully discussed, or one discussed and two others covered partially. Whilst there will be gaps, there should only be an occasional error.
3	One area discussed and one discussed partially, or all three covered partially. There are likely to be several errors and omissions in the discussion.
2	Only one area discussed or makes a partial attempt at two areas.
1	None of the three areas covered without significant error.
0	No relevant analysis.

examples of the points made in the response

- E_k proportional to ω^2
- E_k proportional to I
- for same mass of tram I or ω increased but not mass of flywheel

Shape

- I depends on mass and distribution of mass around axis
- ($I = \sum mr^2$ so) arrange more m at outer edge of flywheel
- by using heavy rim and spokes/thin centre web
- increase radius

Material

- use higher density material at rim
- use material of higher tensile strength / breaking stress

- for higher speeds without bursting/to withstand rotational/centripetal stresses
- eg titanium, CFRP

Design for high ω - increase ω by:

- reduce friction at bearings
- use lubrication or roller bearings/air bearings/magnetic bearings
- smooth outer surfaces / encase in vacuum
- small increase in ω gives large increase in E_k (because ω^2)

Also allow

- sketches which convey correct info clearly
- use of 'depends on' for 'proportional to'
- need for perfect balance
- gyroscopic effects